# Bridging Adversarial Robustness and Semi/Self/Un-supervised Learning

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### 1 Introduction

Deep learning has achieved state-of-the-art performance on many pattern recognition tasks [4]. Nonetheless, a series of recent work show that deep neural networks are typically vulnerable to adversarial perturbations in a relative small scale [8], which means a human-imperceptible perturbation can violate the prediction of modern machine learning models easily. As a natural result, great concerns are posed for researcher to find defensive algorithms for robust and stable models. One of the most successful methods, known as adversarial training [6], use strong adversarial examples as data augmentation to solve a minimax game:

$$\min_{\theta} \mathbb{E}_{(x,y)\sim\mathcal{D}} \max_{\|\eta\| \le \epsilon} \ell(\theta; x + \eta, y).$$
(1)

where  $\ell$  is the cross entropy loss,  $\mathcal{D}$  is training dataset and  $\theta$  is the parameters of model.

On the other hand, many learning settings have emerged with the fast development of machine learning, including semi/self/un-supervised learning which are under different scenarios according to different label information provided. However, it turns out that we there is subtle but important connection between them and adversarial robustness. The most crucial point is that

Clean data and adversarial data can be seen as two different data source domains.

With this insight, many training methods can be proposed naturally to boost the robustness of deep learning models.

## 2 Bridging Adversarial Robustness and Existing Learning Methods

#### 2.1 Semi-supervised Learning

Virtual adversarial training (VAT) [7], is one of the most classical semi-supervised learning algorithms, it combines two loss term:

$$\mathbb{E}_{(x,y)\sim\mathcal{D}^l}\ell(\theta;x,y) + \lambda \mathbb{E}_{x\sim\mathcal{D}^l} \bigcup_{\mathcal{D}^{ul}} \mathbb{D}\{p(y|x)||p(y|x')\}$$
(2)

to smooth the prediction of classifier on both labeled data  $\mathcal{D}^l$  unlabeled data  $\mathcal{D}^{ul}$ , where x' is a perturbed version of x. With our previously mentioned insight, if we take advantage of this technique into adversarial training, then we have:

$$\min_{\boldsymbol{\theta}} \mathbb{E}_{(x,y)\sim\mathcal{D}}\ell(\boldsymbol{\theta}; x, y) + \lambda \cdot \mathbb{E}_{x\sim\mathcal{D}^l \bigcup \mathcal{D}^{ul}} \mathbb{D}\{p(y|x)||p(y|x')\}$$
(3)

where x' is the *adversarial examples* of original input x. This has been adopted by [2] [12] [10].

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#### 2.2 Self-supervised Learning

In [3], treating the data as unlabeled data, an auxiliary loss proposed in self-supervised learning is used in adversarial training:

$$\ell_{\rm SS} = \frac{1}{4} \left[ \sum_{r \in \{0^{\circ}, 90^{\circ}, 180^{\circ}, 270^{\circ}\}} \ell_{\rm CE}\left(\theta; R_r(x), r\right) \right] \tag{4}$$

where  $R_r(x)$  rotates input x for r degree and a 4-way auxiliary classifier is used to predict the rotation degree r. Combine this with previous adversarial training loss can boost the robustness performance.

#### 2.3 Un-supervised Learning

Here we mainly focus on the application of un-supervised domain adaptation algorithms in adversarial robustness. [9] treat the adversarial examples and clean input data like they are from two different source data domain, trying to make the feature extractor to extract the same feature from these two distributions via additional regularization term from domain adaption field. For example, deep CORAL loss [11], Multi-kernel MMD loss [5] [1] can be used with existing adversarial training technique.

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